

CO₂-CarbonCycle-Climate-Interactions C⁴I

Lauren Gregoire [PDRA/researcher]

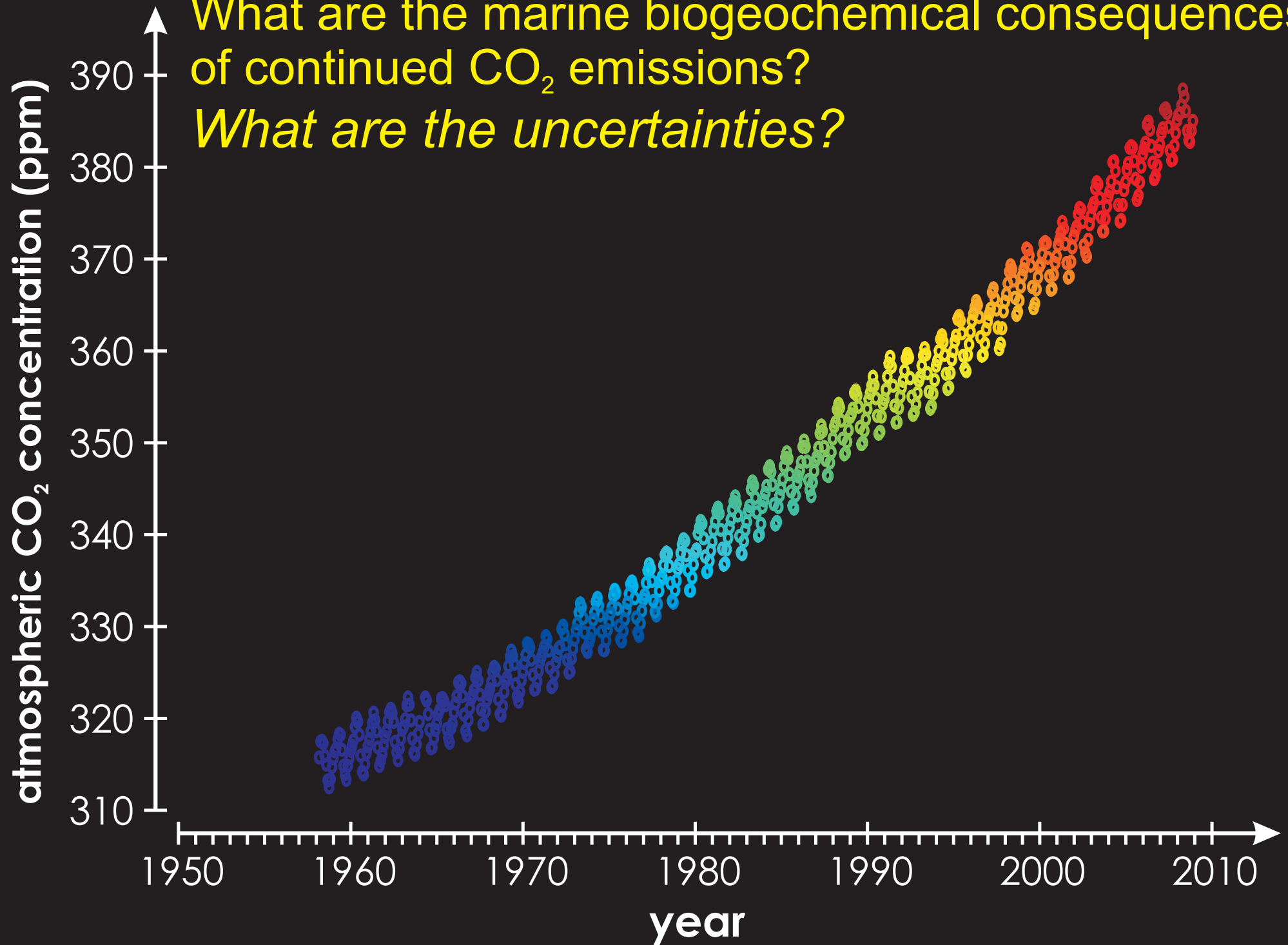
Jamie Wilson [PhD/project student]

Steve Barker

Andy Ridgwell



What are the marine biogeochemical consequences of continued CO₂ emissions?
What are the uncertainties?



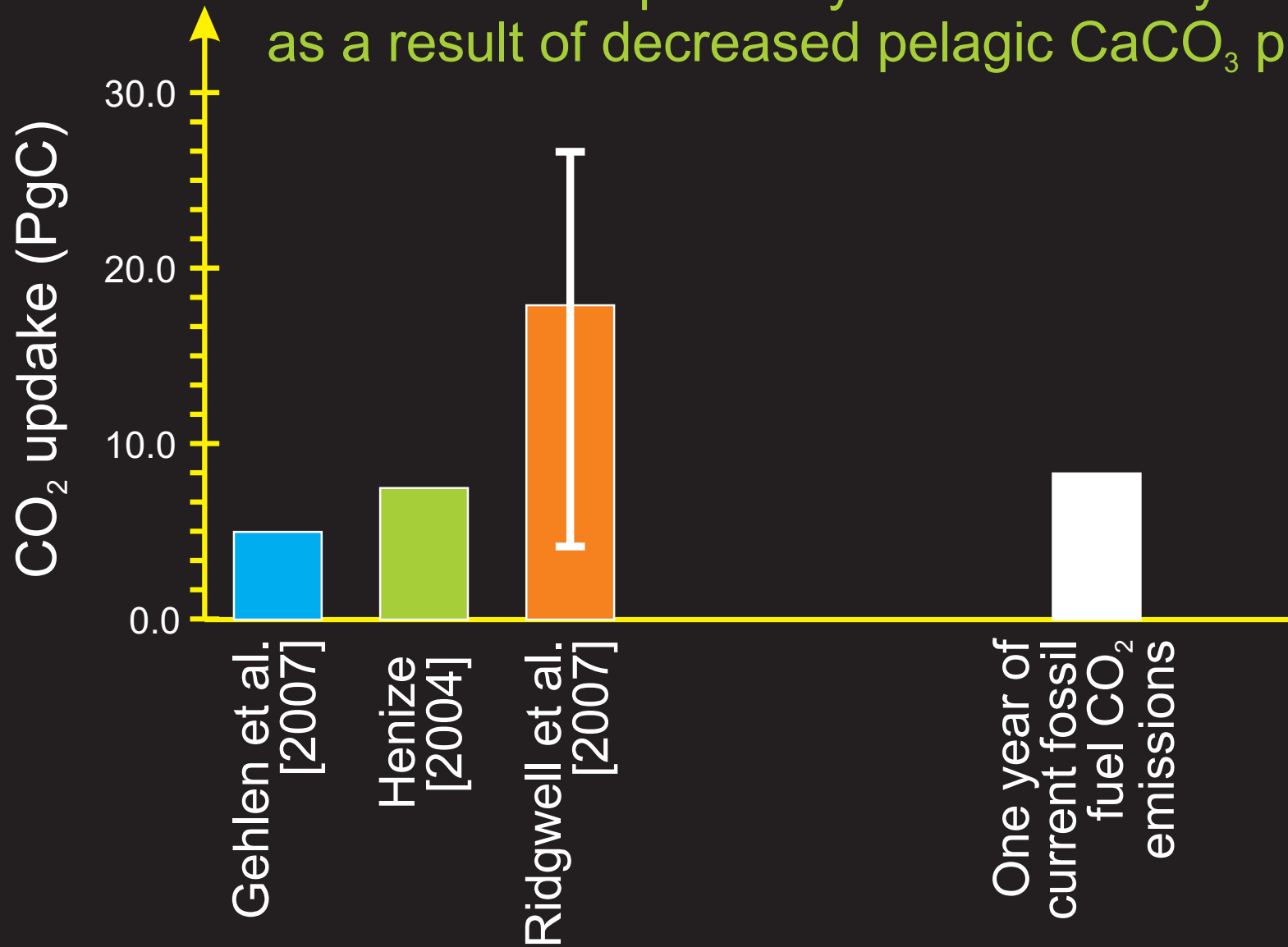
Calcification responses (CaCO_3 per cell per day) at elevated (~ 2 to ~ 3) CO_2

Species	Strain	Year location	Exp. design	Manipulation		Reference
<i>Emiliana huxleyi</i>	PML B92/11A	1992 North Sea	laboratory culture	acid/base	↓	Riebesell et al. [2000] Zondervan et al. [2001]
<i>Emiliana huxleyi</i>	PML B92/11A	1992 North Sea	laboratory culture	acid/base	↓	Riebesell et al. [2000] Zondervan et al. [2001]
<i>Emiliana huxleyi</i>	CAWPO6	1992 South Pacific	laboratory culture	CO_2 bubbling	↑	Iglesias-Rodriguez et al. [2008]
<i>Emiliana huxleyi</i>	MBA 61/12/4	1991 N. Atlantic	laboratory culture	CO_2 bubbling	↑	Iglesias-Rodriguez et al. [2008] (pers com)
<i>Emiliana huxleyi</i>	CCMP 371	1987 Sargasso Sea	laboratory culture	CO_2 bubbling	↓	Feng et al. [2008]
<i>Emiliana huxleyi</i>	CCMP 371	1987 Sargasso Sea	laboratory culture	CO_2 bubbling	↓	Feng et al. [2008]
<i>Emiliana huxleyi</i>	TW1	2001 W. Mediterranean	laboratory culture	CO_2 bubbling	↓	Sciandra et al. [2003]
<i>Emiliana huxleyi</i>	Ch 24-90	1991 North Sea	laboratory culture	CO_2 bubbling	↔	Buitenhuis et al. [1999]
<i>Emiliana huxleyi</i>	CAWPO6	1992 South Pacific	laboratory culture	CO_2 bubbling	↑	Shi et al. [2009]
<i>Gephyrocapsa oceanica</i>	PC7/1	1998 Portuguese shelf	laboratory culture	acid/base	↓	Riebesell et al. [2000] Zondervan et al. [2001]
<i>Calcidiscus leptoporus</i>	AC365	2000 S. Atlantic	laboratory culture	acid/base	↓↑	Langer et al. [2006]
<i>Coccolithus pelagicus</i>	AC400	2000 S. Atlantic	laboratory culture	acid/base	↔	Langer et al. [2006]

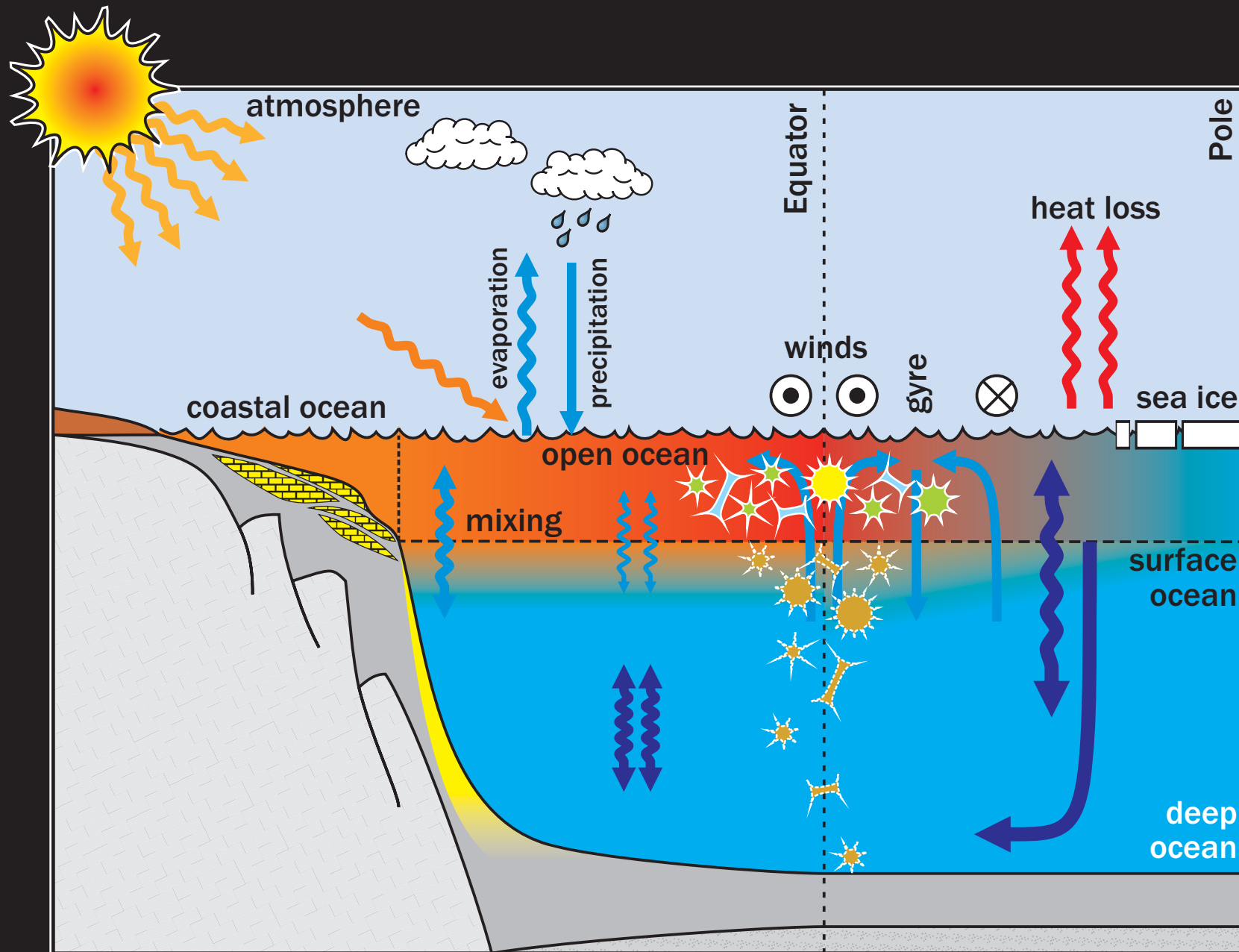
From: Ridgwell et al. [2009] (Biogeosciences)

Global carbon cycle impacts

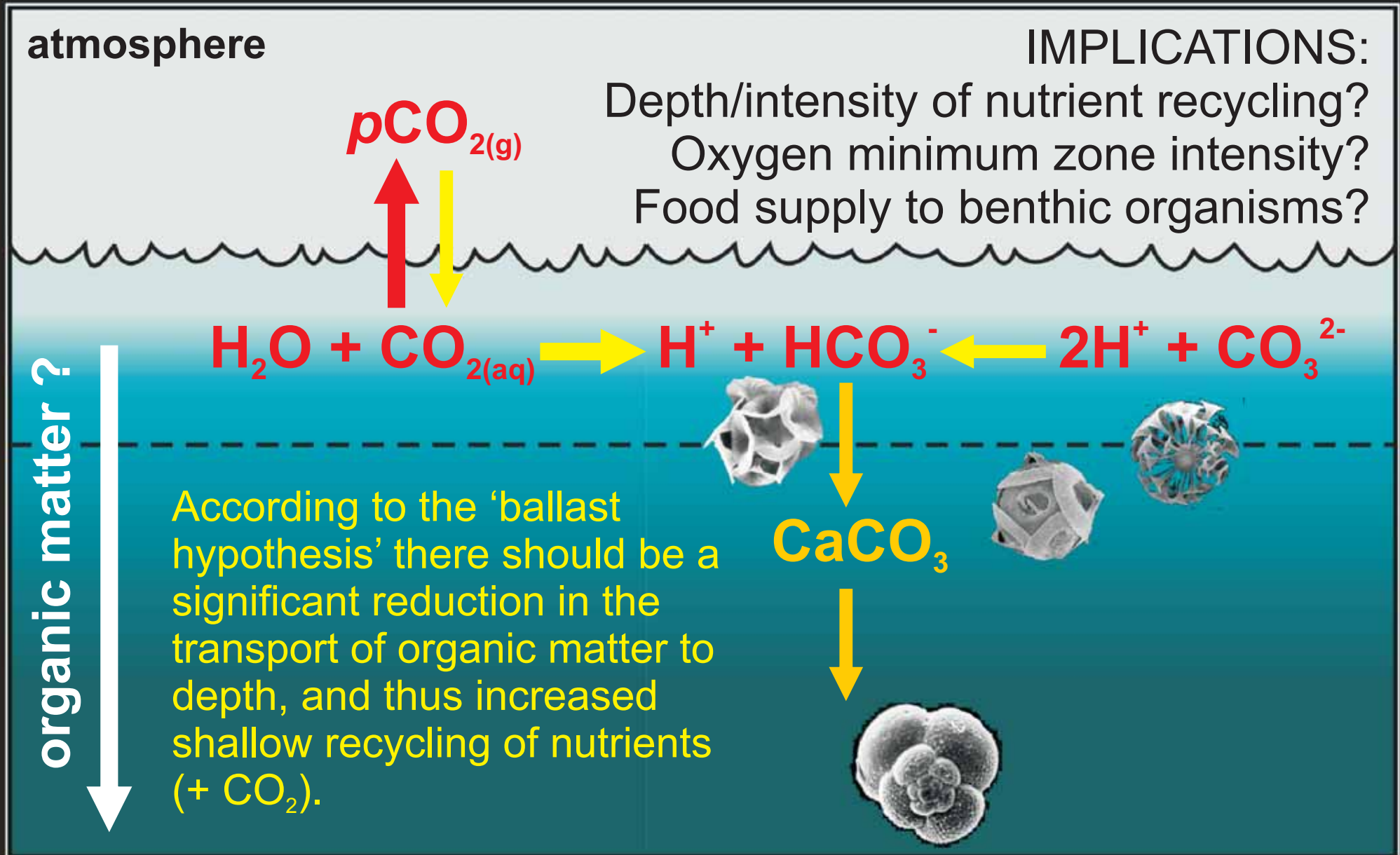
Additional fossil fuel CO₂ removed from the atmosphere by the ocean at year 2100 as a result of decreased pelagic CaCO₃ production



CO₂-Carbon Cycle-Climate-Interactions



Global biogeochemical impacts in a High CO₂ World



$$\mathbf{D} = (\mathbf{d}_1, \mathbf{d}_2, \dots, \mathbf{d}_N) \in \mathfrak{R}^{m \times N}, \quad (6)$$

while the ensemble of perturbations, with ensemble mean equal to zero, can be stored in the matrix

$$\mathbf{E} = (\boldsymbol{\epsilon}_1, \boldsymbol{\epsilon}_2, \dots, \boldsymbol{\epsilon}_N) \in \mathfrak{R}^{m \times N}, \quad (7)$$

from which we can construct the ensemble representation of the measurement error covariance matrix

$$\mathbf{R}_e = \frac{\mathbf{E}\mathbf{E}^T}{N-1}. \quad (8)$$

2.3 Analysis equation

The analysis equation, expressed in terms of the ensemble covariance matrices, is

$$\mathbf{A}^a = \mathbf{A} + \mathbf{P}_e \mathbf{H}^T (\mathbf{H} \mathbf{P}_e \mathbf{H}^T + \mathbf{R}_e)^{-1} (\mathbf{D} - \mathbf{H} \mathbf{A}). \quad (9)$$

Using the ensemble of innovation vectors defined as

$$\mathbf{D}' = \mathbf{D} - \mathbf{H} \mathbf{A} \quad (10)$$

and the definitions of the ensemble error covariance matrices in Eqs. (4) and (8) the analysis can be expressed as

$$\mathbf{A}^a = \mathbf{A} + \mathbf{A}' \mathbf{A}'^T \mathbf{H}^T (\mathbf{H} \mathbf{A}' \mathbf{A}'^T \mathbf{H}^T + \mathbf{E} \mathbf{E}^T)^{-1} \mathbf{D}'. \quad (11)$$

When the ensemble size, N , is increased by adding random samples, the analysis computed from this equation will converge towards the exact solution of Eq. (9) with \mathbf{P}_e and \mathbf{R}_e replaced by the exact covariance matrices \mathbf{P} and \mathbf{R} .

We now introduce the matrix holding the measurements of the ensemble perturbations, $\mathbf{S} = \mathbf{H} \mathbf{A}' \in \mathfrak{R}^{m \times N}$, and we define the matrix $\mathbf{C} \in \mathfrak{R}^{m \times m}$ as

$$\mathbf{C} = \mathbf{S} \mathbf{S}^T + (N-1) \mathbf{R}, \quad (12)$$

and the ensemble approximation, \mathbf{C}_e , of \mathbf{C} as

$$\mathbf{C}_e = \mathbf{S} \mathbf{S}^T + (N-1) \mathbf{R}_e \quad (13)$$

$$= \mathbf{S} \mathbf{S}^T + \mathbf{E} \mathbf{E}^T. \quad (14)$$

Thus, we will consider the use of both a full-rank and exact measurement error covariance matrix \mathbf{R} and the low-rank representation defined in Eq. (8).

The analysis equation (11) can then be written

$$\mathbf{A}^a = \mathbf{A} + \mathbf{A}' \mathbf{S}^T \mathbf{C}^{-1} \mathbf{D}' \quad (15)$$

$$= \mathbf{A} + \mathbf{A} (\mathbf{I} - \mathbf{1}_N) \mathbf{S}^T \mathbf{C}^{-1} \mathbf{D}' \quad (16)$$

$$= \mathbf{A} (\mathbf{I} + (\mathbf{I} - \mathbf{1}_N) \mathbf{S}^T \mathbf{C}^{-1} \mathbf{D}') \quad (17)$$

$$= \mathbf{A} (\mathbf{I} + \mathbf{S}^T \mathbf{C}^{-1} \mathbf{D}') \quad (18)$$

$$= \mathbf{A} \mathbf{X}, \quad (19)$$

where we have used Eq. (3) and $\mathbf{1}_N \mathbf{S}^T \equiv \mathbf{0}$. The matrix $\mathbf{X} \in \mathfrak{R}^{N \times N}$ is defined as

$$\mathbf{X} = \mathbf{I} + \mathbf{S}^T \mathbf{C}^{-1} \mathbf{D}'. \quad (20)$$

2 The EnKF

The EnKF is now briefly described with focus on notation and the standard analysis scheme. The notation follows that used in Evensen (2003).

2.1 Ensemble representation for P

As in Evensen (2003), we have defined the matrix holding the ensemble members $\boldsymbol{\psi}_i \in \mathfrak{R}^n$,

$$\mathbf{A} = (\boldsymbol{\psi}_1, \boldsymbol{\psi}_2, \dots, \boldsymbol{\psi}_N) \in \mathfrak{R}^{n \times N}, \quad (1)$$

where N is the number of ensemble members and n is the size of the model state vector.

The ensemble mean is stored in each column of $\bar{\mathbf{A}}$ which can be defined as

$$\bar{\mathbf{A}} = \mathbf{A} \mathbf{1}_N, \quad (2)$$

where $\mathbf{1}_N \in \mathfrak{R}^{N \times N}$ is the matrix where each element is equal to $1/N$. We can then define the ensemble perturbation matrix as

$$\mathbf{A}' = \mathbf{A} - \bar{\mathbf{A}} = \mathbf{A} (\mathbf{I} - \mathbf{1}_N). \quad (3)$$

The ensemble covariance matrix $\mathbf{P}_e \in \mathfrak{R}^{n \times n}$ can be defined as

$$\mathbf{P}_e = \frac{\mathbf{A}' (\mathbf{A}')^T}{N-1}. \quad (4)$$

2.2 Measurement perturbations

Given a vector of measurements $\mathbf{d} \in \mathfrak{R}^m$, with m being the number of measurements, we can define the N vectors of perturbed observations as

$$\mathbf{d}_j = \mathbf{d} + \boldsymbol{\epsilon}_j, \quad j = 1, \dots, N, \quad (5)$$

which can be stored in the columns of a matrix

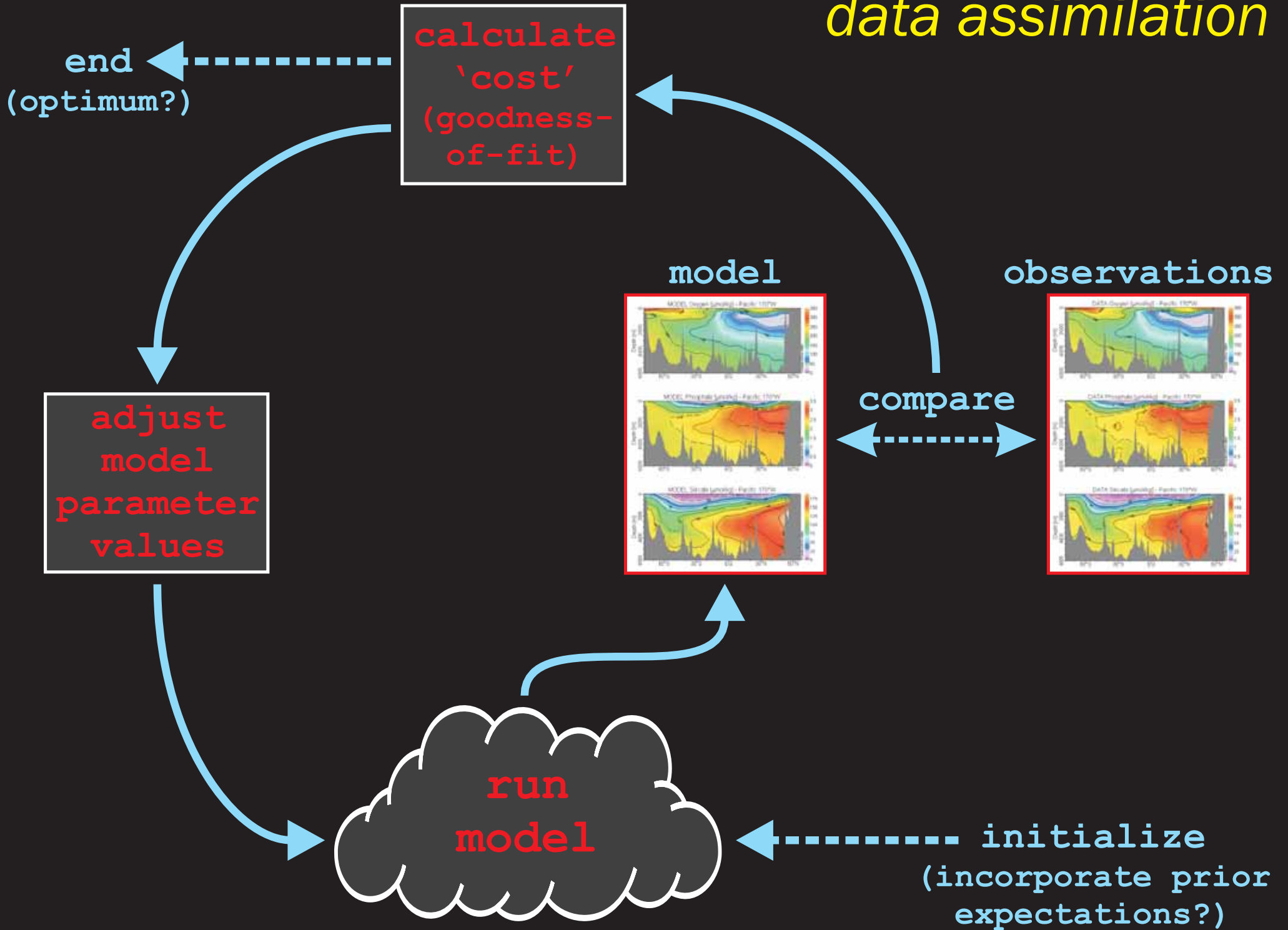
e.g., see:

Evensen [1994] (41 equations)

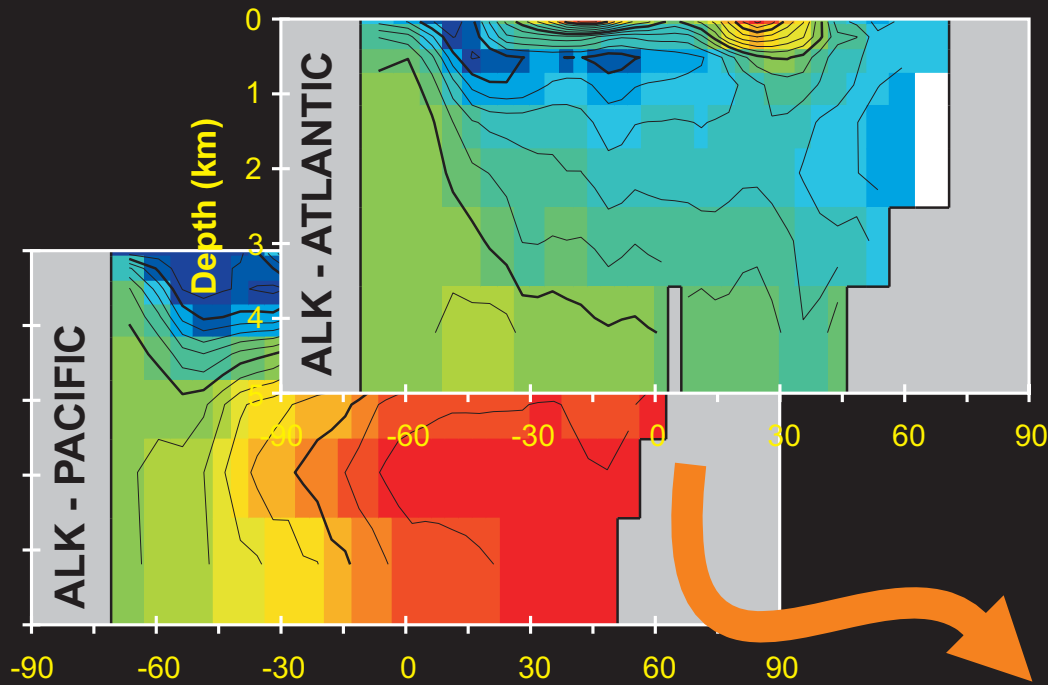
Evensen [2003] (125 equations)

Evensen [2004] (114 equations)

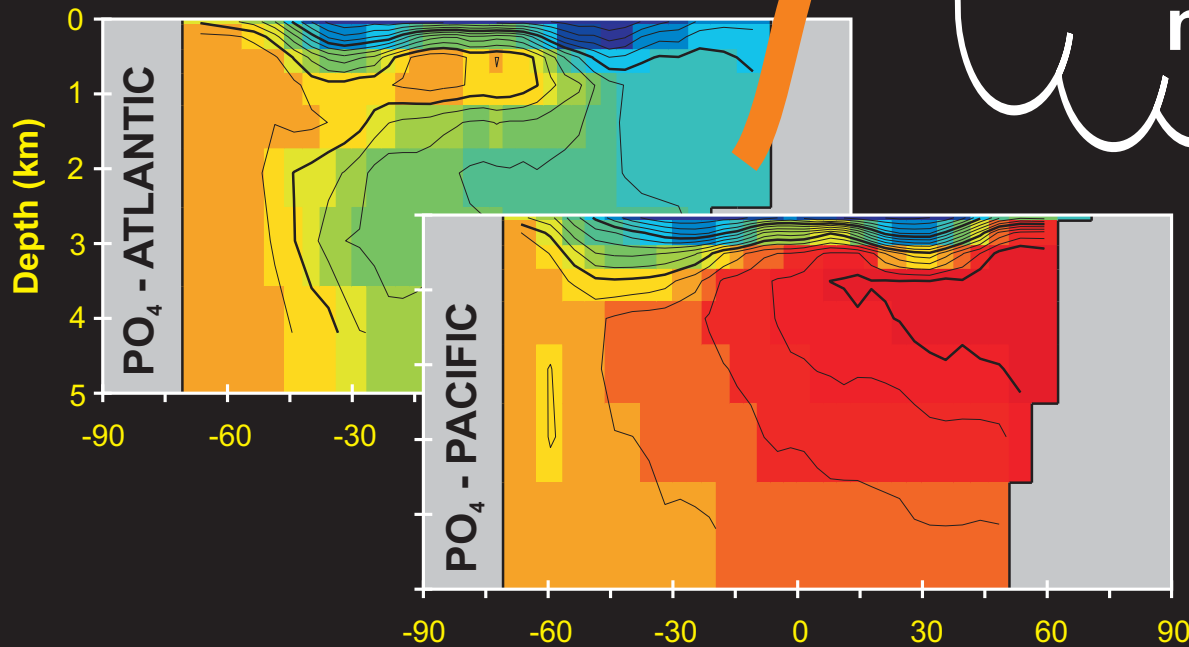
data assimilation



data assimilation



Ensemble Kalman Filter
data assimilation



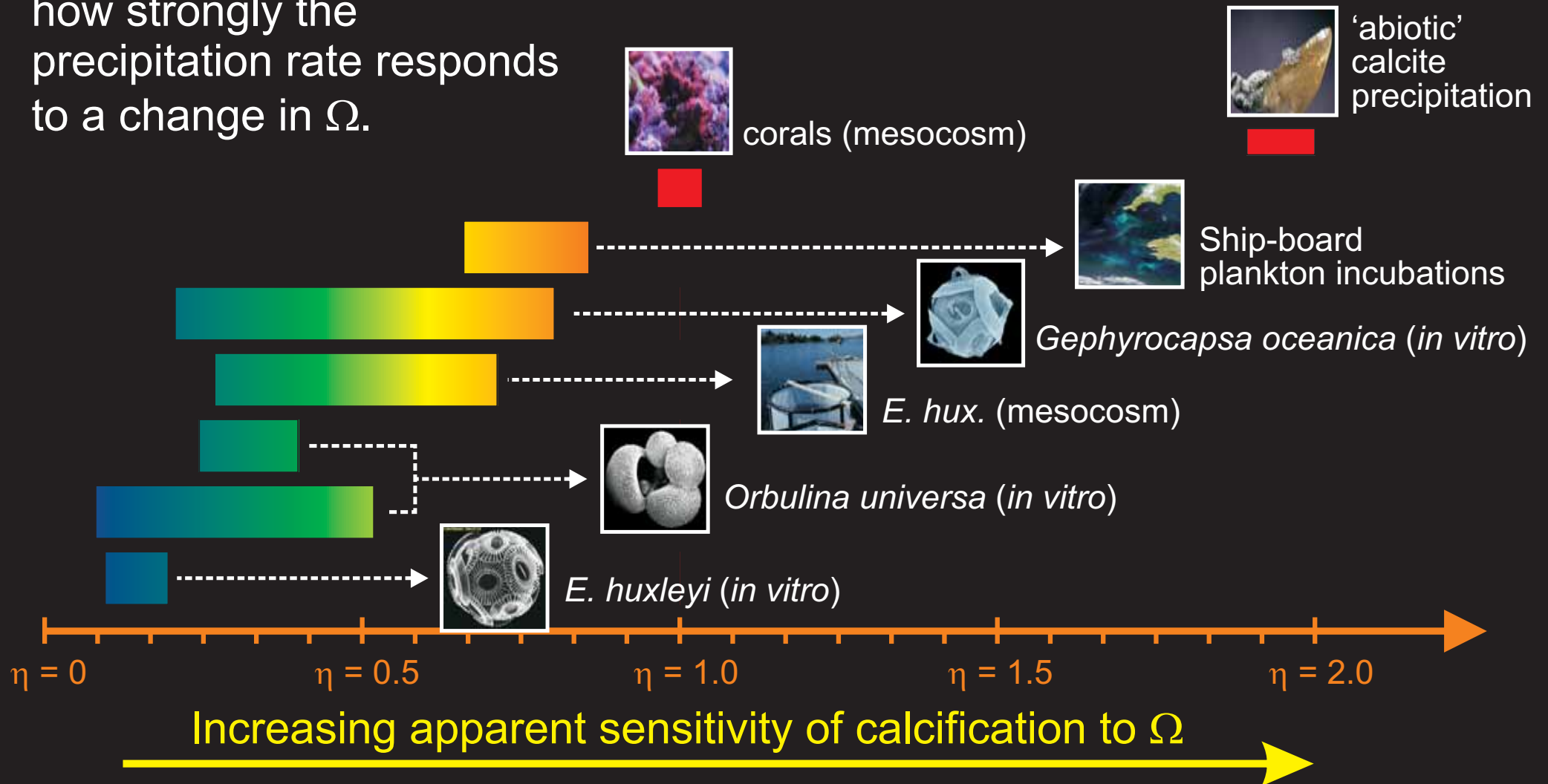
parameterized
 CaCO_3 :POC export
 $\propto K \times (\Omega - 1)^n$

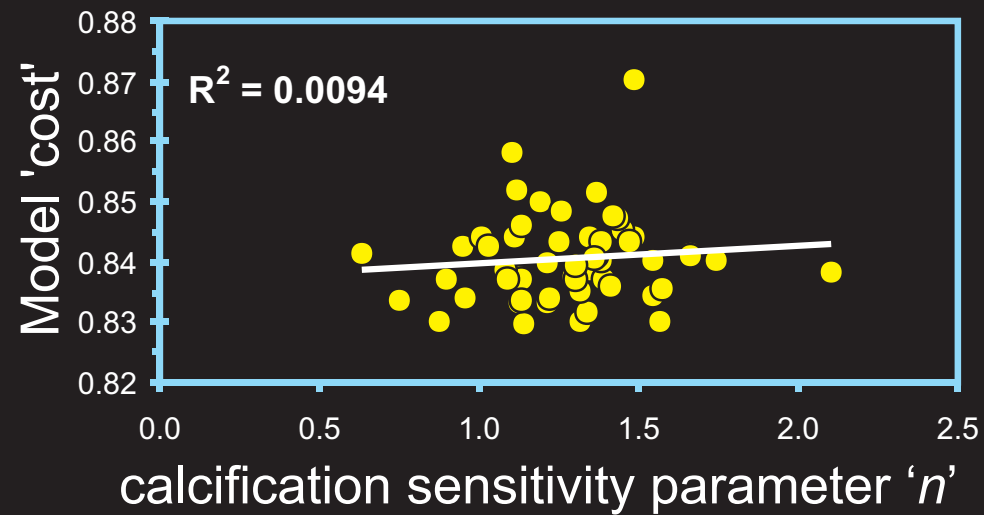
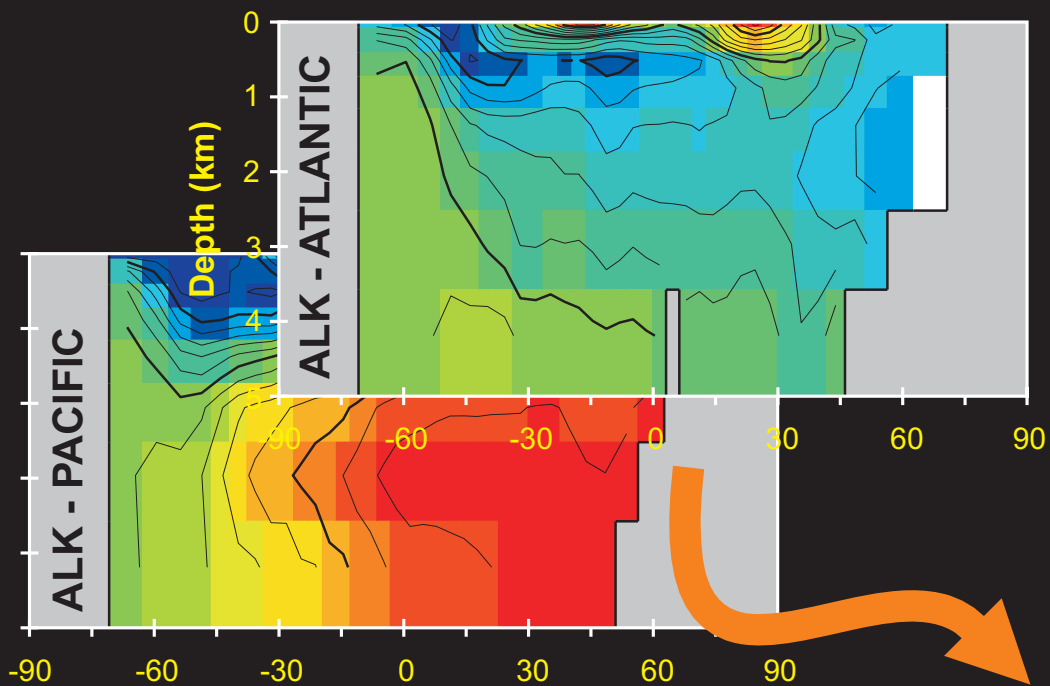
data assimilation

Here, the precipitation of carbonate is described as occurring at a rate;

$$\propto (\Omega - 1)^\eta$$

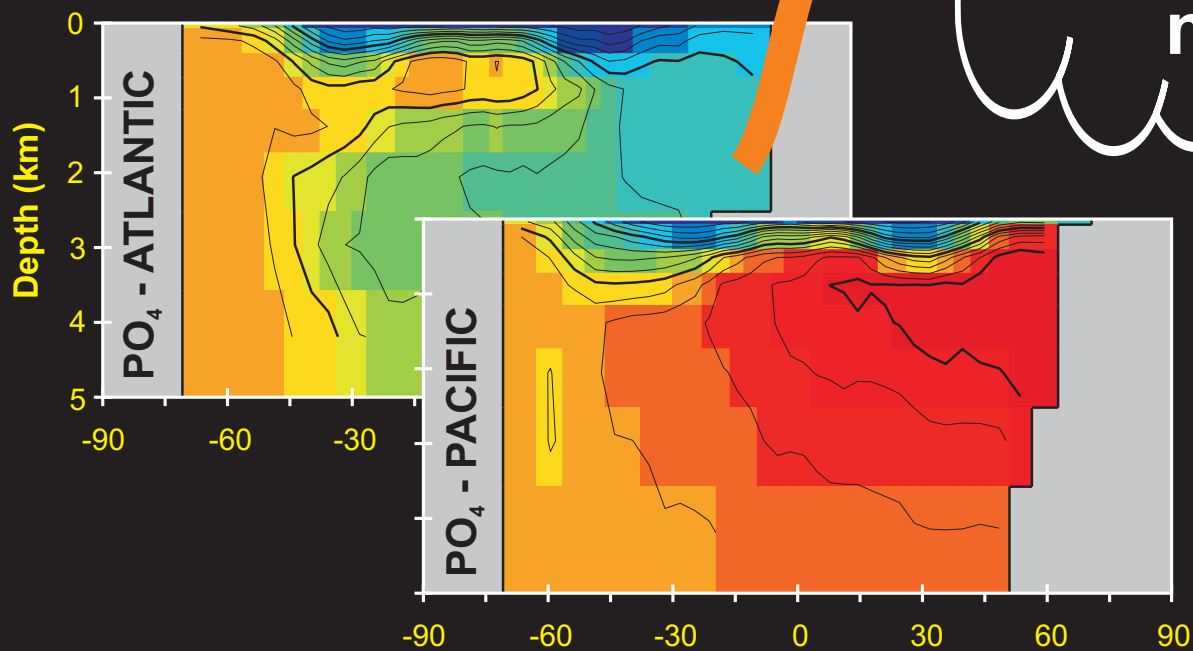
where η is a measure of how strongly the precipitation rate responds to a change in Ω .





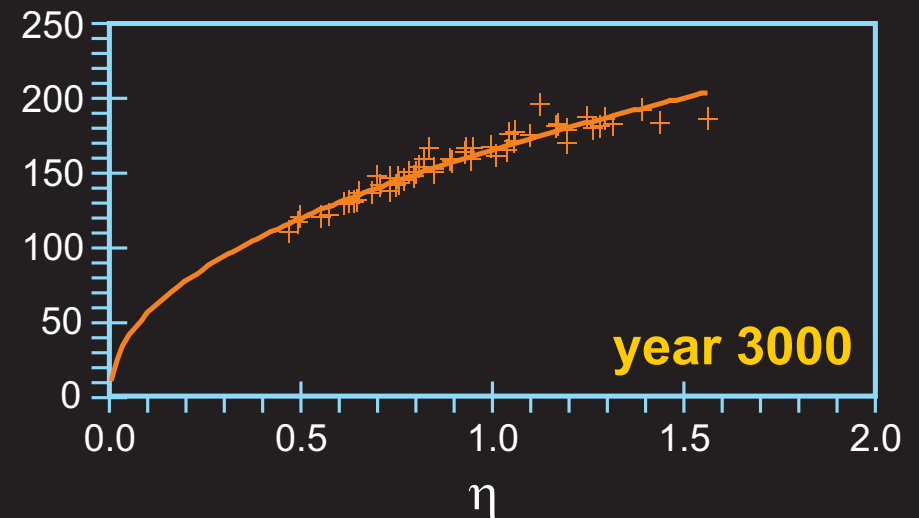
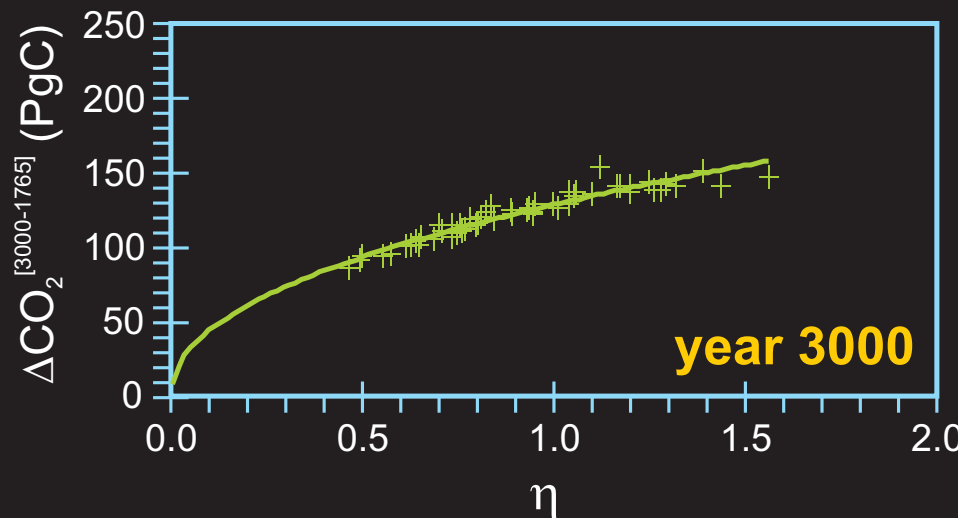
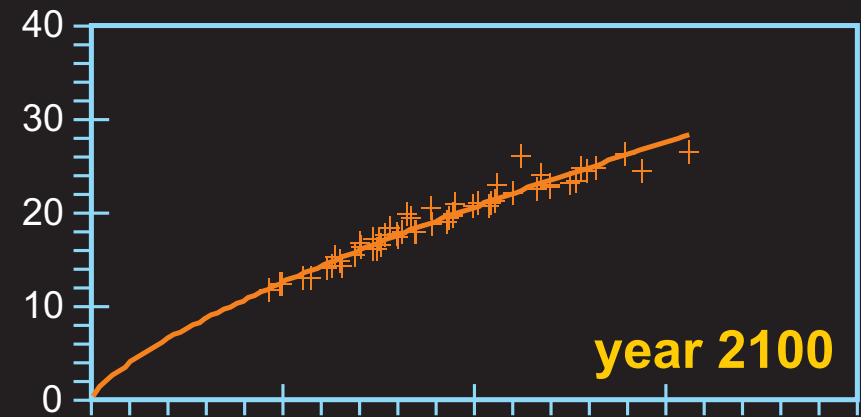
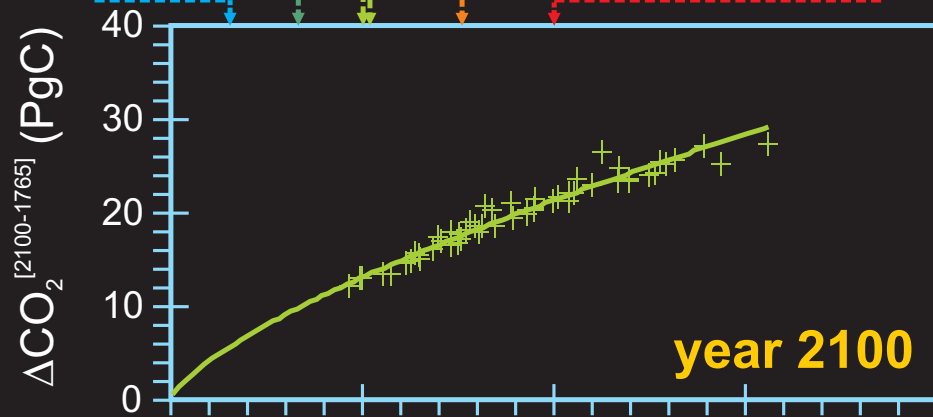
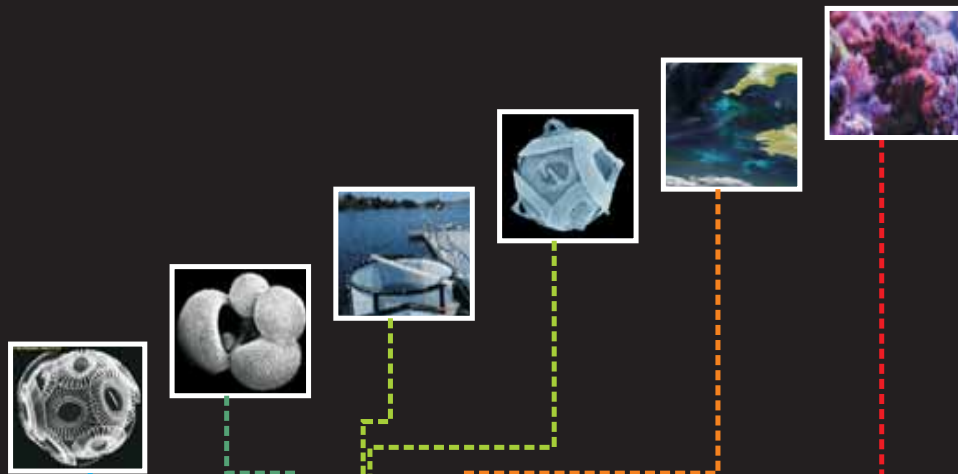
Ensemble Kalman Filter
data assimilation

'GENIE-1'
Earth system
model



parameterized
 CaCO_3 :POC export
 $\propto K \times (\Omega - 1)^n$

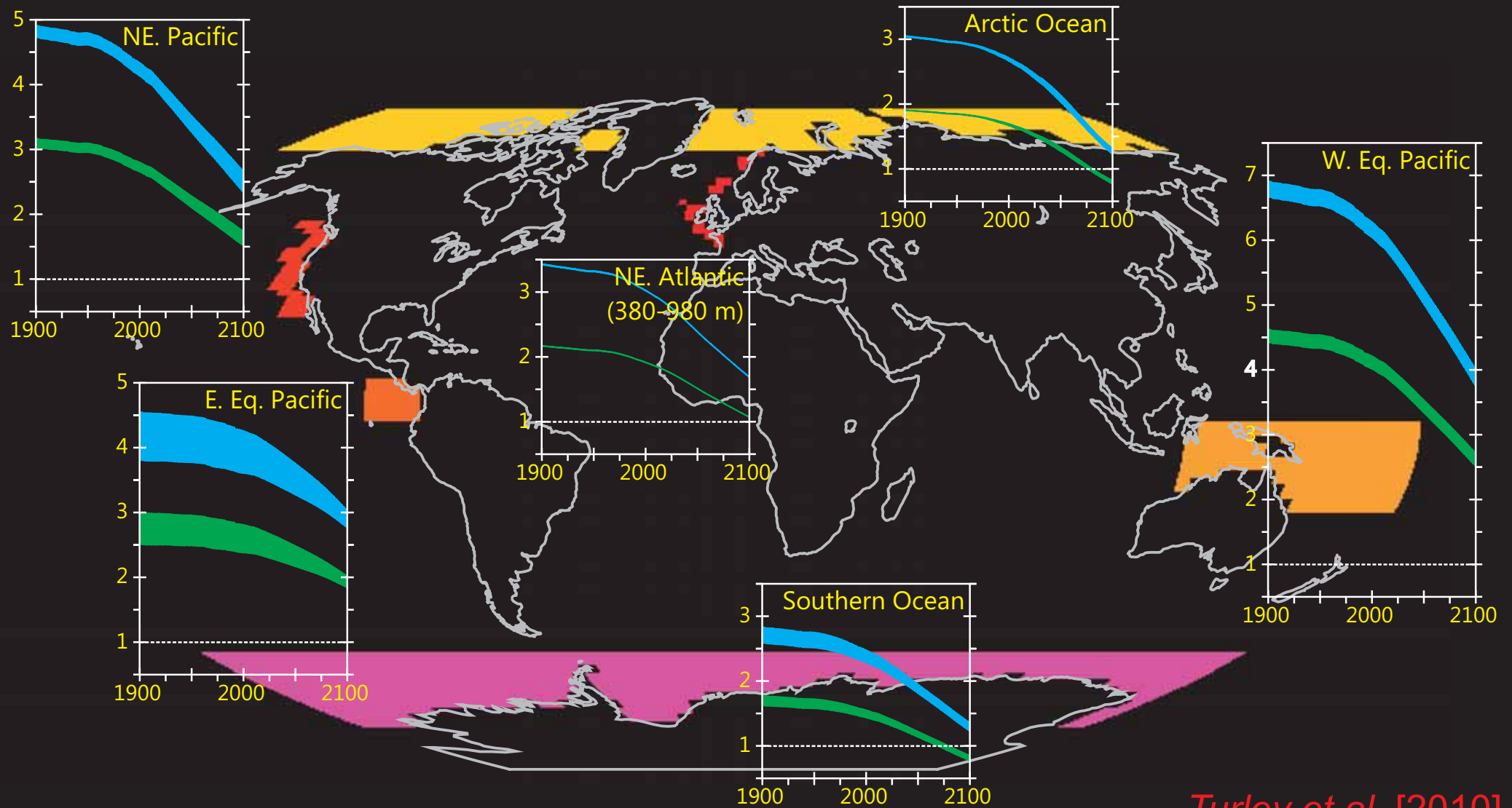
*'projected' uncertainty in
the (atmospheric CO₂)
consequences of ocean
acidification*



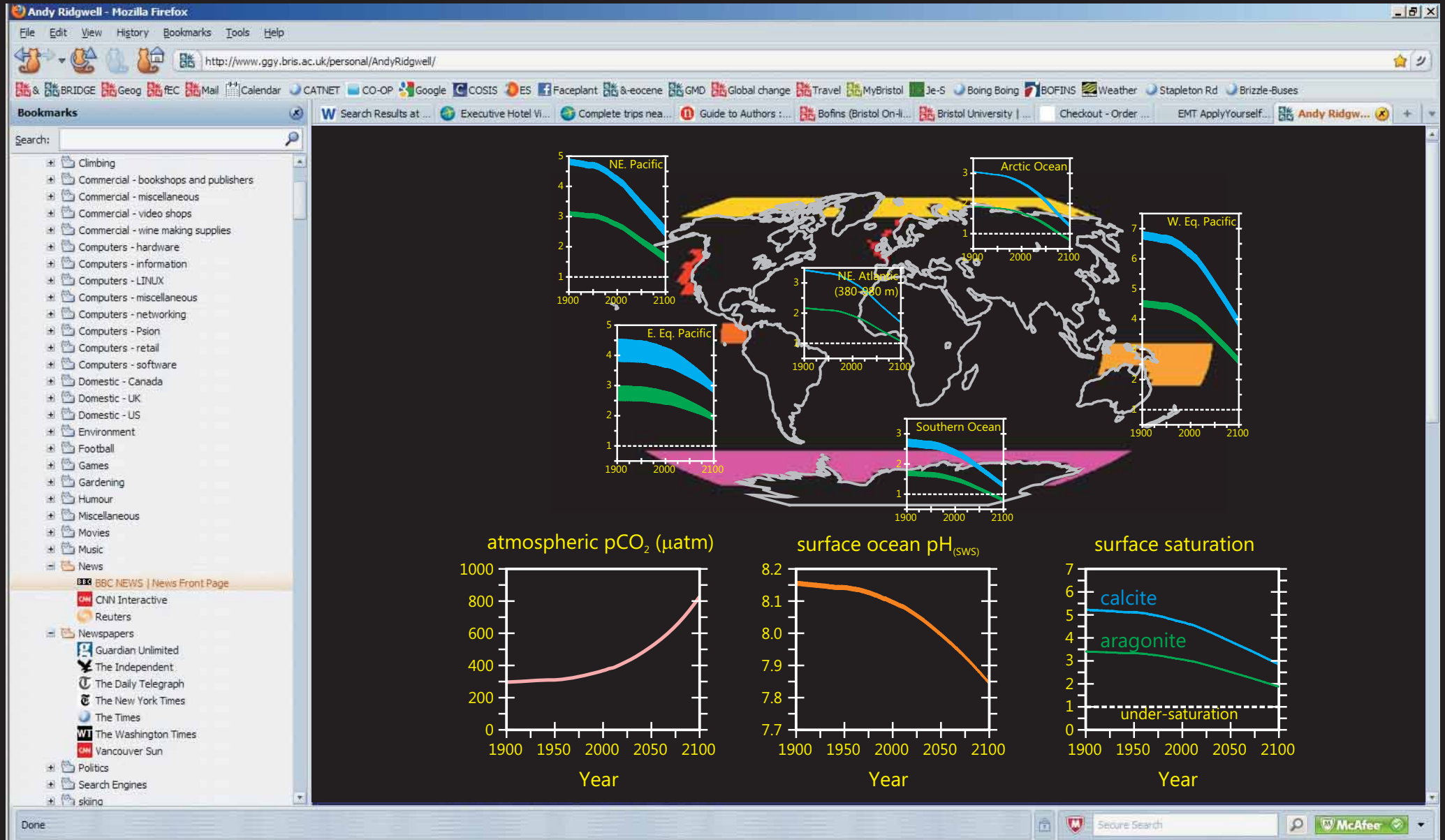
without climate feedback

with climate feedback

Projected (single CO₂ emissions scenario) Seasonal/Regional ocean acidification in the UVic Earth System Model

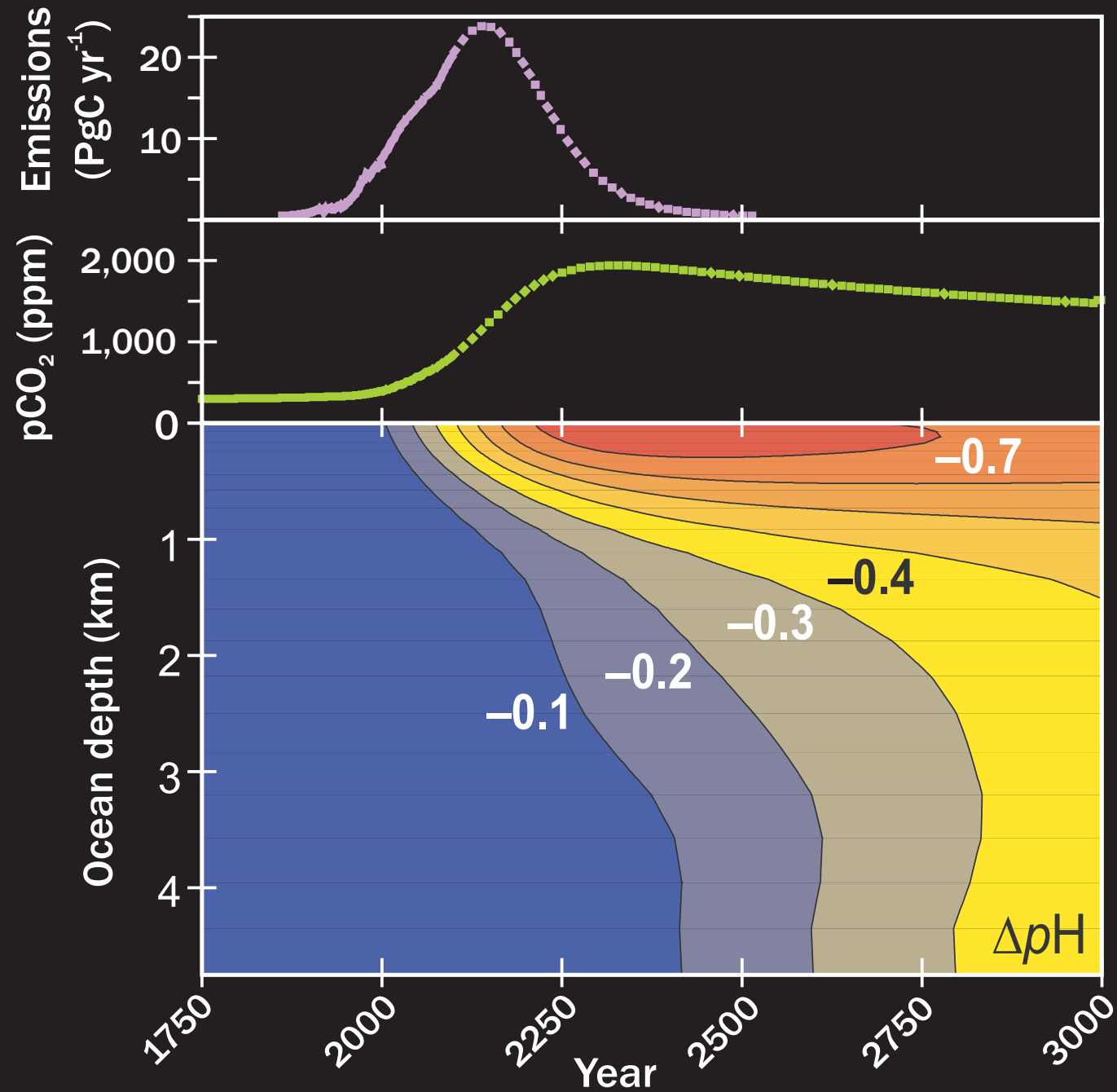


the 'ocean acidification viewer'

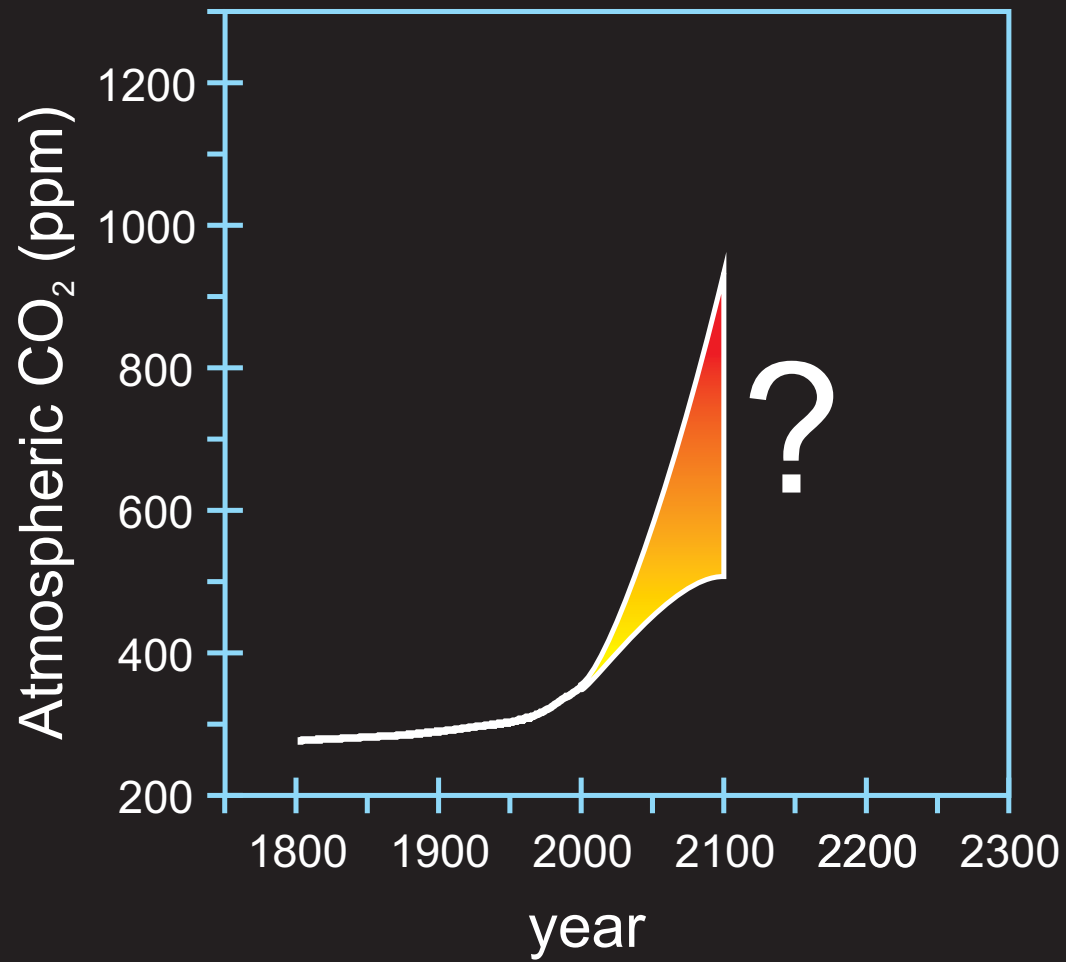




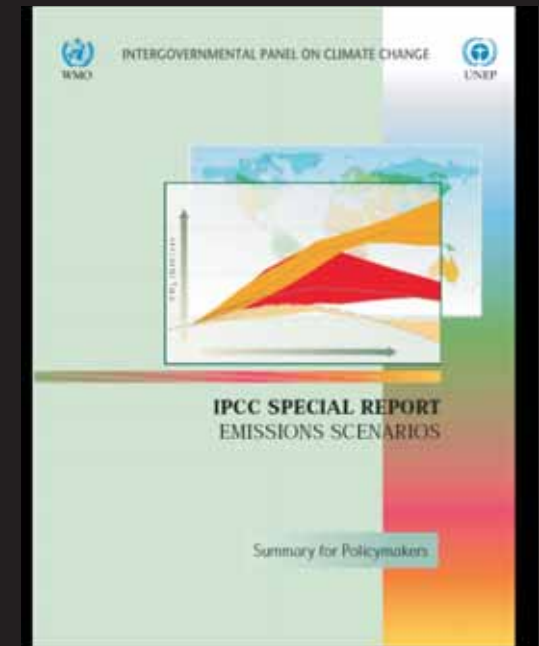
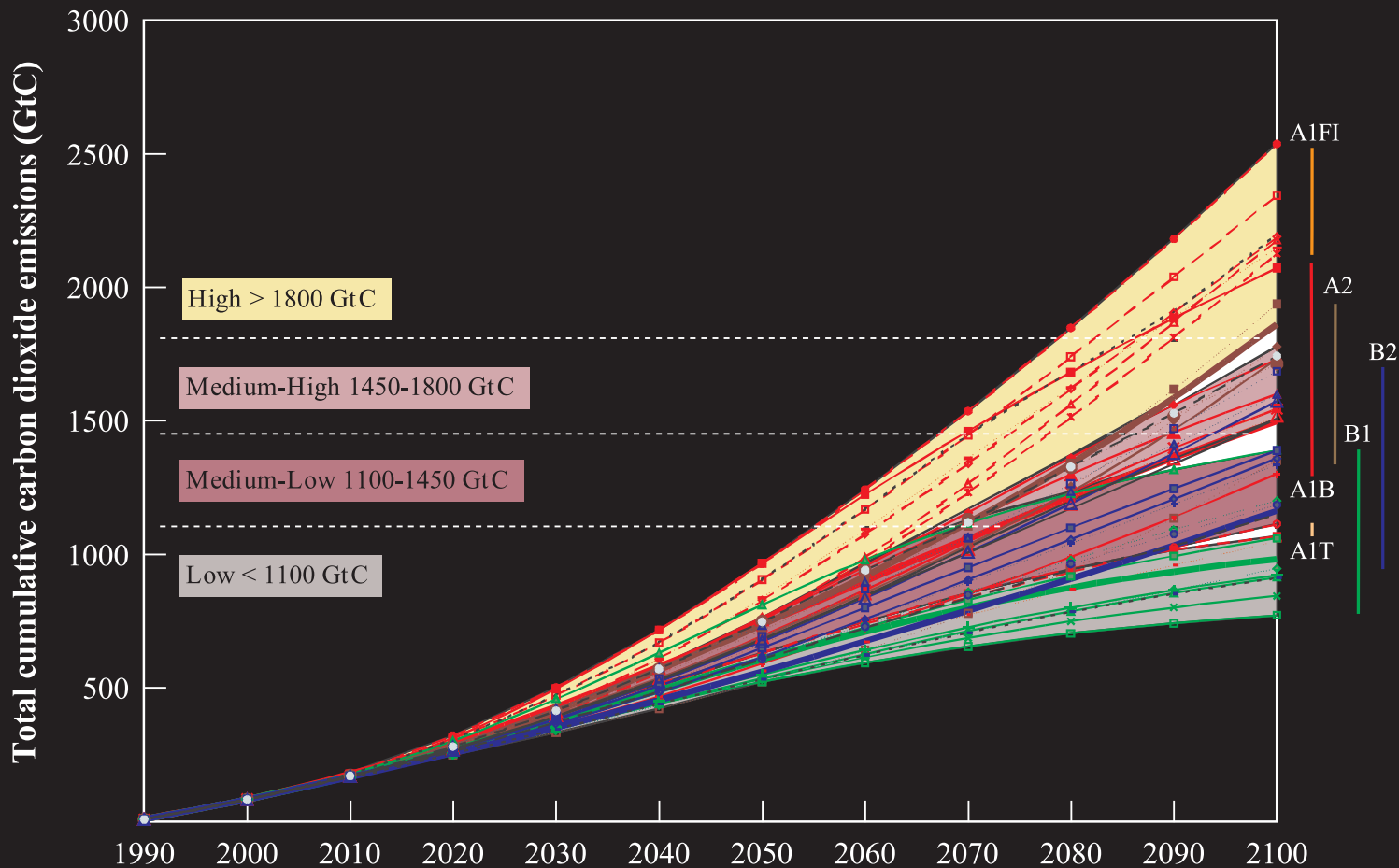
Future trajectories of ocean pH



How will fossil fuel CO₂ emissions change in the future?



What are the uncertainties regarding the (fossil fuel CO₂ emissions) driver of future climate change?



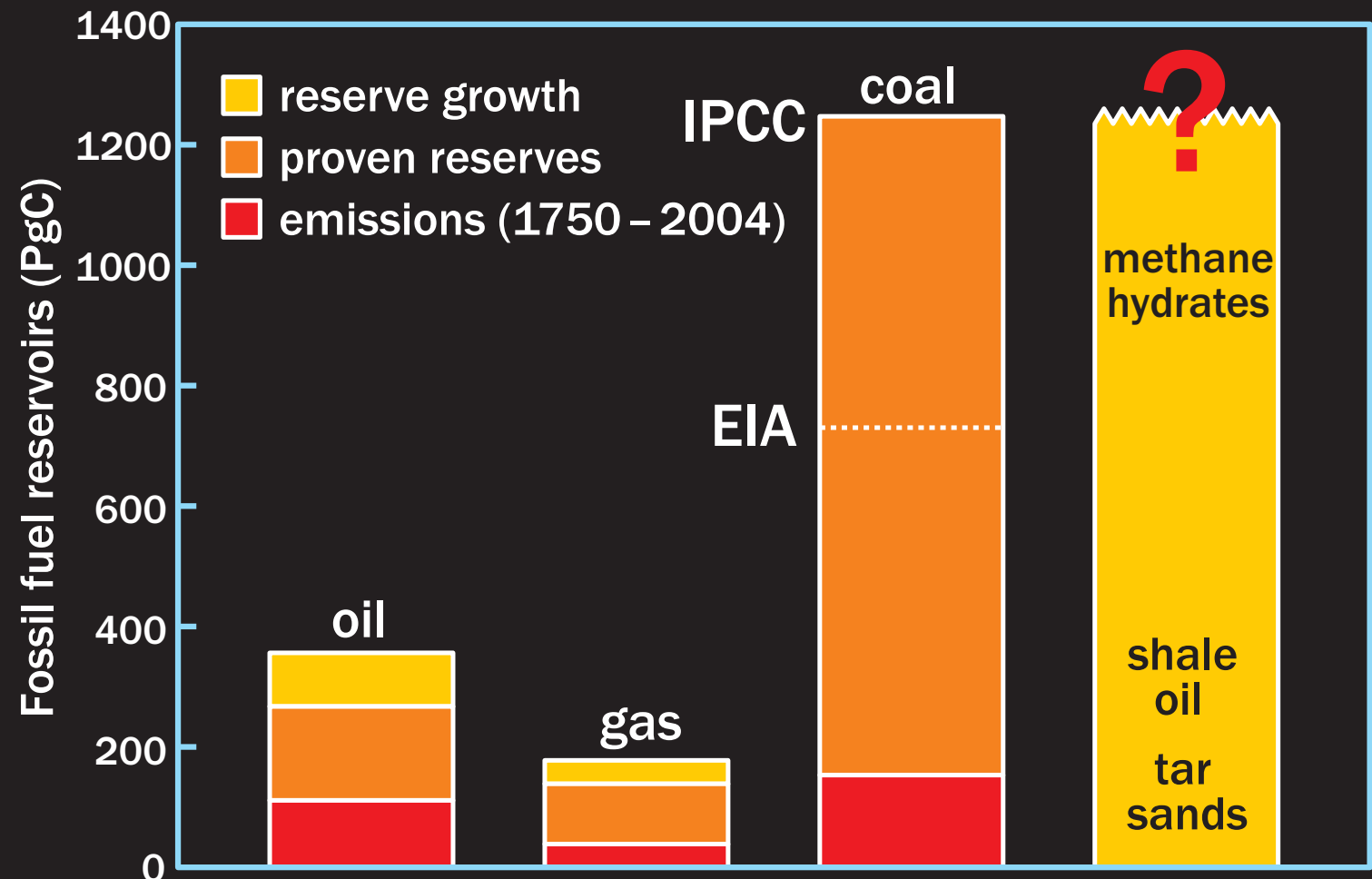
IS92a range

How much carbon can (or will) we burn?

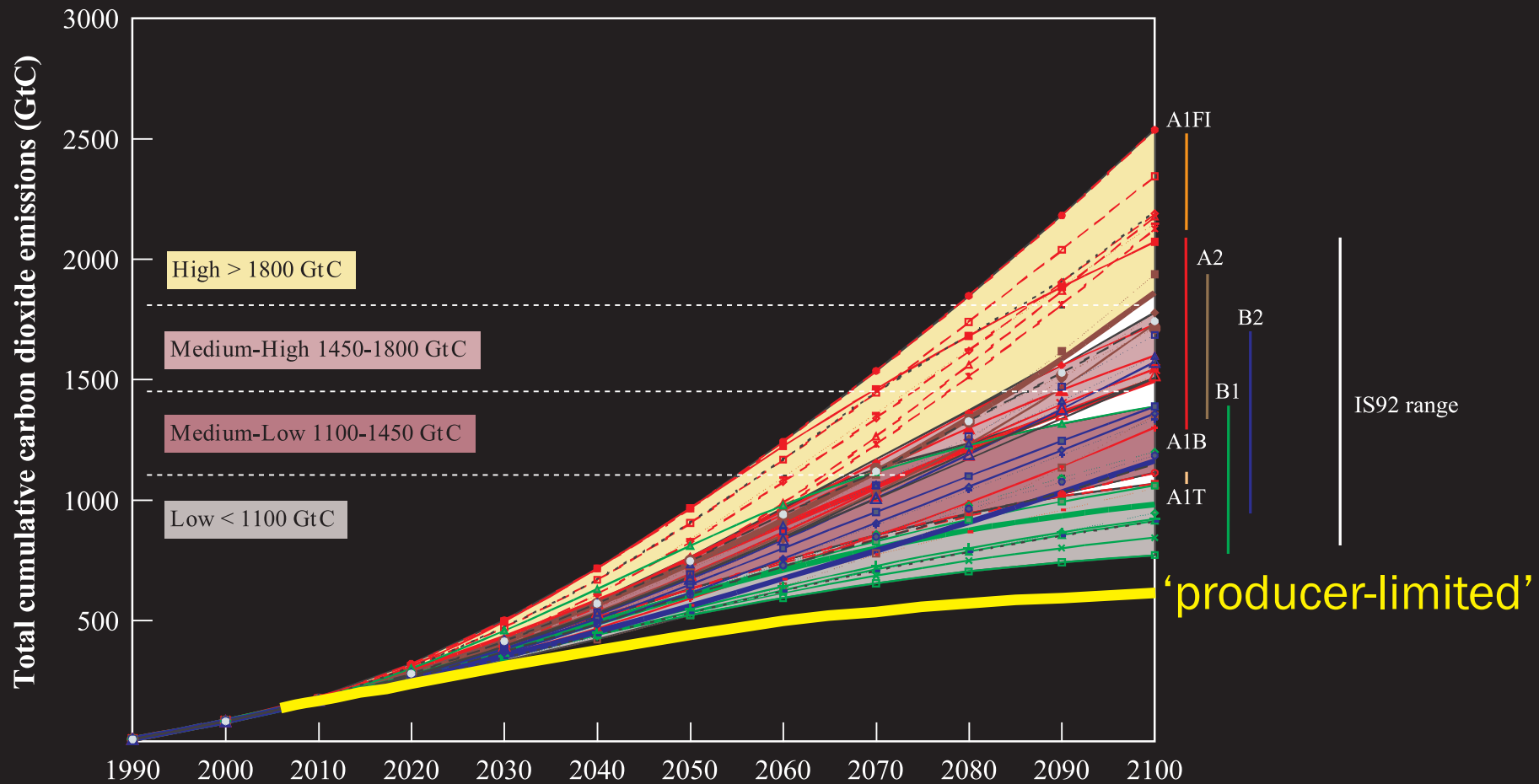
cf.:

~5,000 PgC [Caldeira and Wickett, 2003]

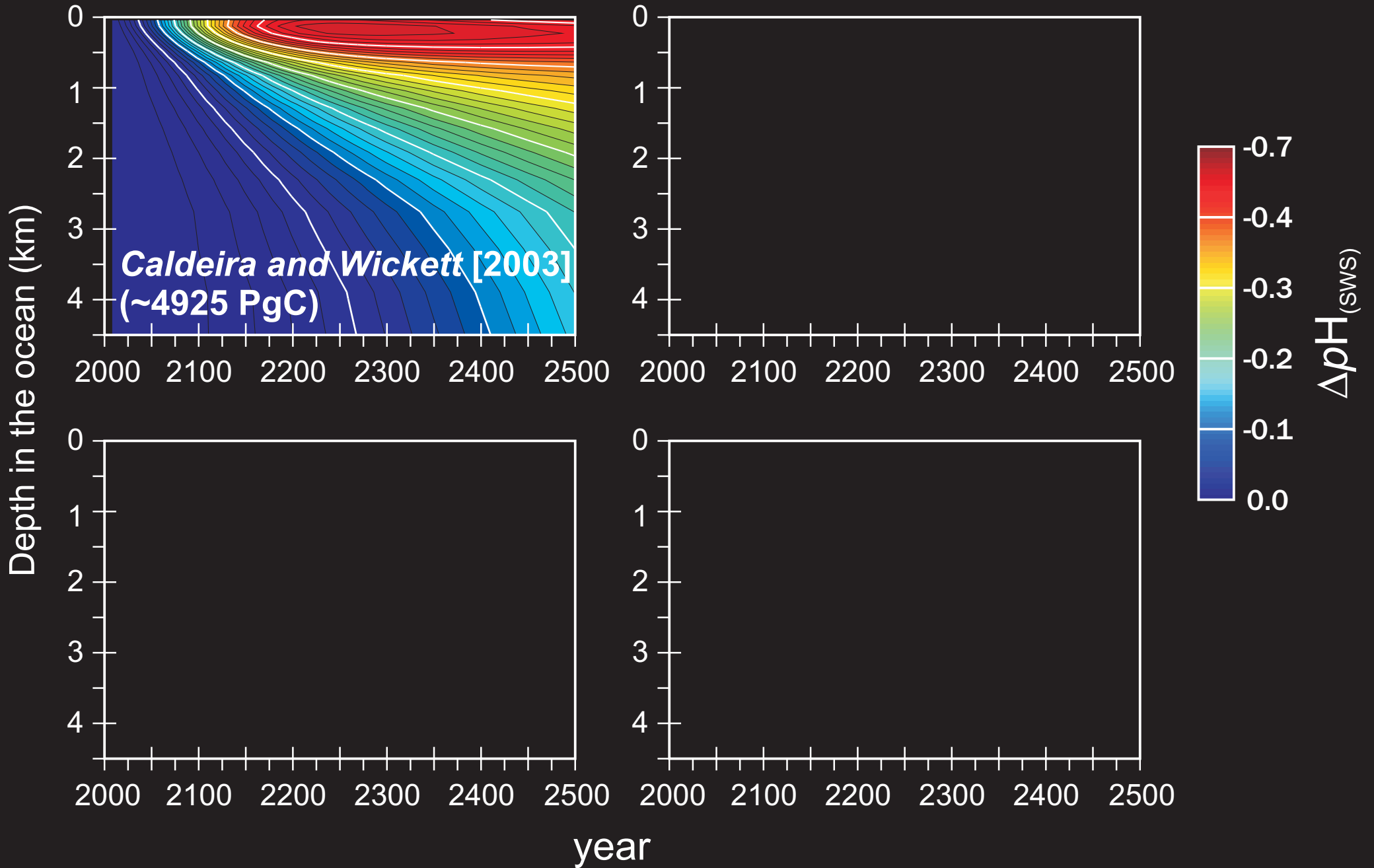
up to 15,000 PgC [Lenton et al., 2006]



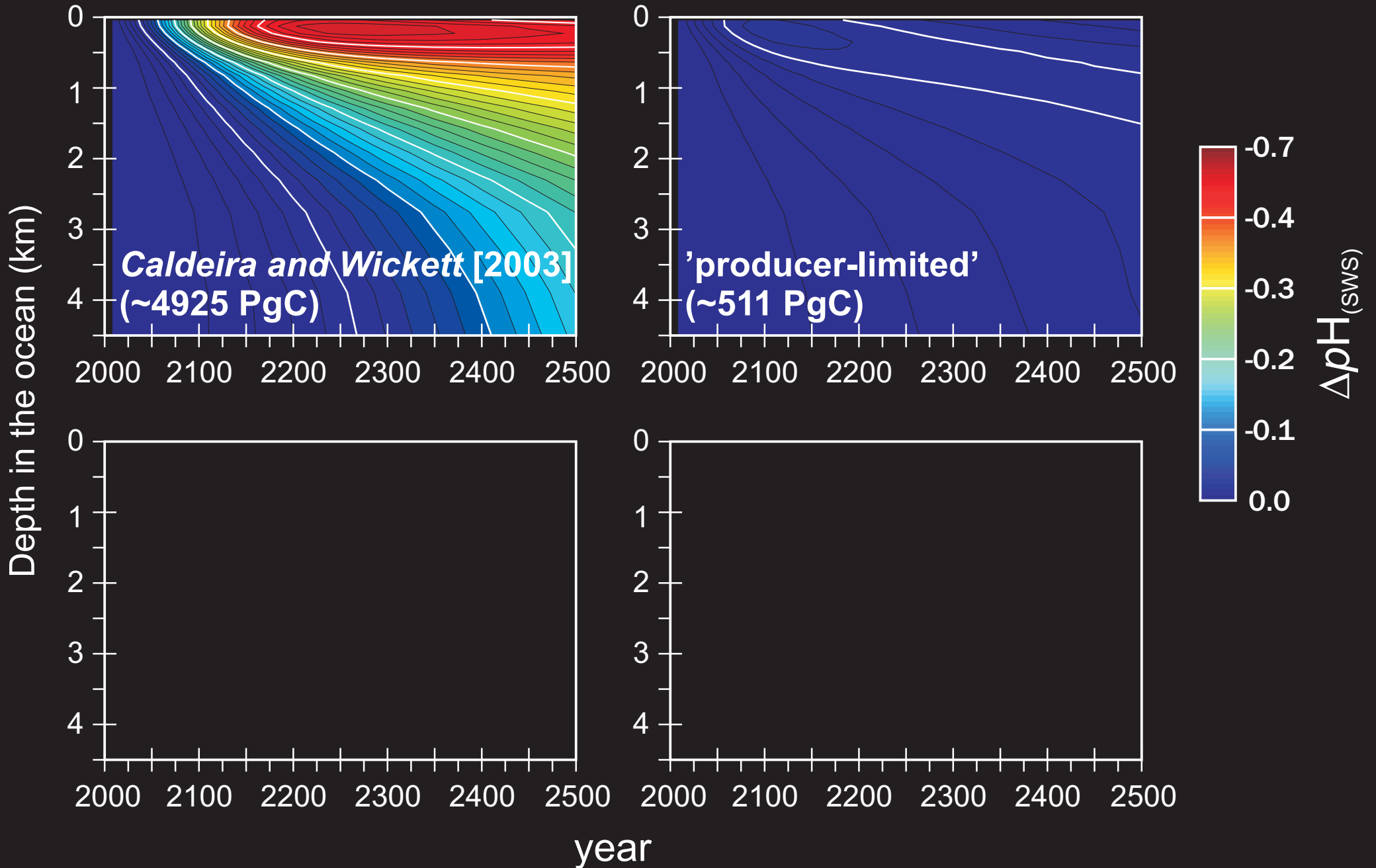
Hubbert's Peak, The Question of Coal, and Climate Change (Dave Rutledge, Caltech)



Future ocean pH projections



Future ocean pH projections



Future ocean pH projections

